

2019

Resolution dependence in an area-based approach to forest inventory with airborne laser scanning

Packalen, Petteri

Elsevier BV

Tieteelliset aikakauslehtiartikkelit

© Elsevier Inc

CC BY-NC-ND <https://creativecommons.org/licenses/by-nc-nd/4.0/>

<http://dx.doi.org/10.1016/j.rse.2019.01.022>

<https://erepo.uef.fi/handle/123456789/7887>

Downloaded from University of Eastern Finland's eRepository

1 **Title** Resolution Dependence in an Area-based Approach to Forest inventory with Airborne Laser
2 Scanning

3 **Authors** Petteri Packalen^a, Jacob Strunk^b, Tuula Packalen^c, Matti Maltamo^d and Lauri Mehtätalo^e

4 ^a petteri.packalen@uef.fi, School of Forest Sciences, Faculty of Science and Forestry,
5 University of Eastern Finland, P.O. Box 111, 80101 Joensuu, Finland. Phone +358-029-445-
6 1111. Corresponding author.

7 ^b jstrunk@fs.fed.us, USDA Forest Service, 3625 93rd Ave SW, Olympia, WA 98512.

8 ^c tuula.packalen@luke.fi, Natural Resources Institute Finland (Luke), Yliopistokatu 6, 80100
9 Joensuu, Finland.

10 ^d matti.maltamo@uef.fi, School of Forest Sciences, Faculty of Science and Forestry,
11 University of Eastern Finland, P.O. Box 111, 80101 Joensuu, Finland.

12 ^e lauri.mehtatalo@uef.fi, School of Computing, University of Eastern Finland, P.O. Box 111,
13 80101 Joensuu, Finland.

14 **Abstract**

15 In an Area Based Approach (ABA) to forest inventories using Airborne Laser Scanning (ALS) data, the
16 sample plot size may vary or the cell size may differ from the plot size. Although this resolution
17 mismatch may cause bias and increase in prediction error, it has not been thoroughly studied. The aim of
18 this study was to clarify the meaning of resolution dependence in ABA, and to further identify its causal
19 factors and quantify their effects. In general, a number of factors contribute to resolution dependence in
20 ABA forest inventories, including the varying point density of the ALS data, the type of response
21 variable, how the predictor variables are computed, and the properties of the prediction model. For
22 quantification, we used field plots with mapped tree locations, which enabled the generation of different
23 sized sample plots inside a larger plot. Plot level above ground biomass (AGB) was the response variable
24 employed in all the models. The error rate seemed to increase when the prediction plots were larger than

25 the fitting plots, and vice versa. The maximum BIAS was 1.50 % and the maximum change of RMSE
26 compared to its value in native resolution was 0.97 % when there was a 4-fold difference in resolution.
27 This indicates that the resolution effect is small in most real-world use cases, however, resolution effect
28 should be carefully considered in ALS-assisted large area inventories that target unbiased estimates of
29 forest parameters.

30 **Funding**

31 This research did not receive any specific grant from funding agencies in the public, commercial, or not-
32 for-profit sectors.

33 **Keywords**

34 Scale dependence, resolution invariance, Airborne laser scanning, Forest inventory, Lidar

35 **Introduction**

36 *Resolution dependence*

37 The construction of a spatial model often involves the specification of input parameters at some chosen
38 spatial scale, i.e. resolution. The resolution may vary with model predictions and may be different from
39 that used in the model construction. This is quite typical in remote sensing and a large number of studies
40 have addressed this issue from different point of views (e.g. Strahler et al., 1986; Turner et al., 1989;
41 Raffy, 1992; Marceau and Hay, 1999; Simic et al., 2004; Chasmer et al., 2009). In general, the conversion
42 from a high resolution to a lower resolution is called *upscaling* and the conversion from low resolution to
43 a higher resolution is analogously called *downscaling* (Liang, 2004). Several authors have proposed
44 frameworks in order to solve scaling problems and compensate for scaling effects (Wu and Li, 2009).

45 The terms *scale* and *resolution* refer to different concepts that depend on the context, discipline, and
46 author. In ecology, for example, the concept of *scale* often refers to the extent and the concept of
47 *resolution* to grain size, but there is not necessarily a connection between the grain size and spatial

48 resolution. In some studies, however, spatial scale refers to the grain size or the grain size is assumed to
49 be equal to the spatial resolution, i.e. pixel size. Correspondingly, *scale invariance* and *resolution*
50 *invariance* are interpreted differently depending on the circumstances. In this study, we will use the term
51 *resolution* to refer to grain size, although in some previous remote sensing studies the term *scale* was used
52 to refer to more or less the same concept (e.g. Zhao et al., 2009). We will explain later in greater detail
53 what resolution means in the context of our study.

54 *Area-based approach to forest inventory*

55 Forest inventories employing Airborne Laser Scanning (ALS) data have become common in many
56 countries (Nilsson et al., 2017). The ALS-based forest inventory methods (Hyypä et al., 2008) can be
57 divided into two groups: the area-based approach (ABA) (Means et al., 2000; Næsset, 2002; Magnussen
58 et al., 2013) and single-tree detection (Hyypä et al. 2001; Koch et al., 2006; Lähivaara et al., 2014).
59 Operational forest inventories employing ALS data are most often implemented with the ABA (Maltamo
60 et al., 2014, chapters 11-13). In ABA, metrics used as predictor variables are calculated from the ALS
61 returns within a plot or grid cell. Using training plots with field-measured stand attributes, a model is
62 formulated between the stand attributes and ABA metrics. This model is then used to predict the stand
63 attributes for each grid cell. A model is typically based on linear (Næsset, 2002) or non-linear regression
64 (Packalén et al., 2011), but non-parametric regression techniques, such as k nearest neighbor (Hudak et
65 al., 2008) and artificial neural networks (Niska et al., 2010), have also been used. A large proportion of
66 studies have focused on forest management inventories (e.g. Næsset, 2004; Packalén and Maltamo, 2007),
67 but a large number of studies have also focused on statistical inference and sampling designs (e.g. Chirici
68 et al., 2016; Gregoire et al., 2016). In forest management inventories, cell level predictions are typically
69 aggregated to the stand level (Næsset, 2004), whereas in large area strategic inventories, cell level
70 predictions may be used as auxiliary information either in sampling design or in the estimation phases
71 (Grafström et al., 2017; Strunk et al., 2012).

72 Several factors that affect the performance of ABA have been studied, such as the number of sample plots
73 (Junttila et al., 2013), plot positioning error (Gobakken and Næsset, 2009), ALS echo density (Thomas et
74 al., 2006), ALS sensor and flying configurations (Keränen et al., 2016), and seasonal effects (Næsset,
75 2005). The effect of sample plot size has also been addressed in many studies (Gobakken and Næsset,
76 2008; Frazer et al., 2011; Ruiz et al., 2014). In general, a reduction in prediction error with larger plot
77 sizes is expected due to spatial averaging of errors (Goetz and Dubayah, 2011). Chen et al. (2016) showed
78 within a coherent framework that AGB prediction error decreases as plot size increases, and determined
79 the relative contributions of each error source.

80 Resolution issues in ABA originate from the use of non-constant size plots and/or cells. The most
81 convenient option is use the same sized plots and cells, but this is not always possible. There are several
82 reasons why an analyst may have a need to deal with data at different resolutions:

- 83 1) *Sample plot sizes vary.* It is common to measure sample plots of different sizes in a range of
84 forest types to maximize the efficiency of field work – small plots in young or homogeneous
85 forests, and large plots in sparse, mature or heterogeneous forests. A similar approach is used in
86 some ABA inventories.
- 87 2) *Cell sizes vary.* It may be desirable to split cells (corresponding plot size) into pieces and merge
88 them with neighboring cells. This approach is useful if we want to avoid “mixed” cells in stand
89 borders in order to reduce prediction errors on borders. For example, grid cells located on the
90 border between a sapling and a sawlog stand may greatly overestimate timber volume or mean
91 diameter in the saplings.
- 92 3) *Sample plot size is different to cell size,* although plots are of similar size and cells are of similar
93 size. For instance, an end user may require a certain grid cell size, but an existing set of sample
94 plots or measurement protocols must be used e.g. for economic reasons.
- 95 4) *A combination of cases 1, 2 and 3.*

96 The effect of varying resolution in the ABA arena is an almost unexplored field of study. Zhao et al.
97 (2009) developed methods for the scale-invariant estimation of forest biomass using functional regression
98 models. The models are called functional regression models because the predictors, namely canopy height
99 distribution (CHD) and canopy height quantile functions (CHQ), are themselves functions or functional
100 data. The CHD and CHQ were computed from a ALS-derived canopy height model (CHM) rather than
101 from the ALS point cloud. There are also ABA studies that address resolution or scale but from an
102 entirely different viewpoint than this study. For example, Magnussen et al. (2016) demonstrated a
103 statistical method for upscaling ABA predictions in cases where the response variable is not additive,
104 whereas Chen et al. (2016) proposed a new uncertainty analysis method built on model-based inference
105 that can characterize biomass uncertainty across multiple spatial resolutions. Our study is distinct from
106 the previous research because we clarify the factors that cause resolution issues in a typical ABA, and
107 with an empirical setting, we evaluate how serious the consequences might be if the requirements of
108 resolution invariance are violated. There is a need to understand more thoroughly the resolution
109 dependence in the ABA arena. For instance, we did not find any studies that discuss the resolution issues
110 that originate from the irregular point pattern of ALS data.

111 *Regular or irregular point spacing?*

112 We examine resolution effects in the context of ABA wherein metrics are computed from an ALS point
113 cloud, in contrast to the majority of remote sensing studies where resolution issues are addressed in the
114 context of raster images. This distinction is important: an image is a regular tessellation whereas ALS
115 data are irregularly spaced in a horizontal domain. When metrics are computed from images, the number
116 of observations (i.e. pixels) is constant per unit area. In an irregular point pattern, such as ALS data, the
117 point density per unit area varies. The implication of areas with higher and lower point densities is that
118 areas with higher point density are more heavily weighted than areas with lower point density. For
119 example, let us assume that the left side of a rectangular grid cell has a double point density compared to
120 the right side and a computed metric is e.g. the mean height of points. The mean value of the metric over
121 the cell area is then equal to:

122
$$\frac{2 \times \text{mean height of the left side} + 1 \times \text{mean height of the right side}}{2+1} . \quad (1)$$

123 However, there is no reason to assume that areas with a higher point density are more important than
124 areas with a low point density. The un-equal weighting is simply an undesirable consequence of
125 irregularities in the data acquisition process that can result, for example, from scan pattern, varying
126 scanning angle, or overlapping flight lines. The effects of variable point density on ABA inference are
127 also resolution dependent because the weighting scheme for points within cells also changes as the
128 resolution changes. For example, when the resolution becomes finer, areas with low point density are less
129 likely to be combined with high point density areas.

130 *Objectives*

131 The overall aim of this study is to clarify the meaning of resolution dependence in the context of ABA, to
132 identify the underlying causal factors, and to quantify their effects. Our study design enables us to
133 examine the effects of using up to nine-fold differences in plot and cell sizes. Specific objectives are:

- 134 • To identify requirements for resolution invariance.
- 135 • How do the bias and error rates behave when the requirements of resolution invariance are
136 violated?
- 137 • What is the direction and magnitude of bias with the commonly used ALS height percentiles
138 when the resolution is changed?
- 139 • To present a simple approach to achieve resolution invariance in ABA by considering varying
140 point density.

141 **Theoretical background**

142 *Definition of resolution invariance*

143 Consider a situation where a predictive model based on field plots is used to make prediction for a large
144 area. In principle, we examine two alternatives to compute the prediction for the area: (1) Divide the area

145 to cells of a certain size (e.g. 15 x 15m), compute the predictors for each cell and use them for predictions,
146 and average or sum the cell-level predictions over the cells. (2) Compute the predictors directly for the
147 whole area and apply them for the whole area as if it were one cell. We define *resolution invariance* in
148 ABA to mean that both approaches will yield an identical prediction. In this study, we focus on resolution
149 discrepancy common in practice due to a resolution mismatch between the plot area used in model fitting
150 and the area covered by a cell from an ALS-derived predictor grid. We do not assume that the least
151 squares model coefficients are identical when fitted at the different resolutions, but instead look at the
152 behavior of predictions when fitted at one resolution and used for predictions at a different resolution. In
153 this study, we only consider continuous response variables, although the theory and findings partly apply
154 to categorical response variables as well.

155 *Resolution invariant ABA model*

156 Consider a situation where spatial resolution affects the values of ALS-derived metrics only through the
157 number of ALS echoes, which is fixed and proportional to cell size. This is true in a grid where the
158 number of ALS echoes per grid cell is the same for all cells of a given size. Obviously, this is not the case
159 in most real world applications, because ALS data consist of irregularly spaced echoes in horizontal
160 space.

161 Consider a case where the cells of area a_i (e.g. 625 m² in Figure 1, left panel) are formed by k_i non-
162 overlapping subcells of areas a_{ij} (e.g. 156.25 m² in Figure 1, mid panel or 69.44 in the right panel), so
163 that $a_i = \sum_{j=1}^{k_i} a_{ij}$. The forest attribute for cell i is y_i and for its subcell j it is y_{ij} . Variable y is said to be
164 additive if $a_i y_i = \sum_{j=1}^{k_i} a_{ij} y_{ij}$. The measures of mean or total quantity per area unit: total volume, above
165 ground biomass, basal area and number of stems, are additive. Measures of mean or total quantity per
166 tree: dominant height, mean height or mean diameter, for example, are not additive. There are, however,
167 special cases when the mean diameter or height of trees is additive, this happens whenever the number of
168 trees per area unit is constant.

169 Consider a metric x_{ij} , which is based on the ALS measurements of the canopy on subcell j within the

170 larger cell i . It is typically the mean of echo heights, a certain quantile of the echo heights, or proportion
171 of echoes above, below, or between fixed heights. A metric is said to have a *resolution invariant mean* if
172 the (optionally) weighted mean of subcell metrics is equal to the metric computed for the entire cell i :

$$173 \quad \sum_{j=1}^k w_{ij} x_{ij} = x_i, \quad (2)$$

174 where weights w_{ij} is rescaled subcell area a_{ij} , scaled such that subcell-level weights sum to one at cell-
175 level:

$$176 \quad w_{ij} = \frac{a_{ij}}{\sum_{j=1}^k a_{ij}}. \quad (3)$$

177 Assuming a grid where the number of ALS echoes per cell and subcell is constant, a_{ij} can be
178 alternatively the number of echoes per subcell. Some ALS metrics satisfy the condition of a resolution
179 invariant mean, such as the mean height of echoes without any height threshold and many metrics of
180 proportion above, below, or between certain fixed heights. Height quantiles are an example of ALS
181 metrics that are not resolution invariant as they are not unbiased for the corresponding population
182 parameters: upper sample quantiles produce an underestimation of the corresponding population quantiles
183 and lower quantiles produce an overestimation. The biases are greatest for the extreme quantiles (Reiss,
184 1989), and are affected by the shape of the underlying distribution of ALS echoes, as well as by the
185 number of ALS echoes. In the ALS arena, quantiles are typically called percentiles and hereafter we will
186 follow this convention.

187 Consider an ABA forest inventory, where the prediction is based on the model:

$$188 \quad y_i = f(x_i; \boldsymbol{\beta}) + e_i, \quad (4)$$

189 where x_i is the vector of ALS metrics in the larger cell i and the residual e_i has a mean of zero. Let us
190 assume that the parameter vector $\boldsymbol{\beta}$ is fixed and known so that:

$$191 \quad E(y_i) = f(x_i; \boldsymbol{\beta}), \quad (5)$$

192 which is the expected value of y_i . The model is called resolution invariant if the weighted sum of subcell-
193 level predictions equals the cell-level prediction:

$$194 \quad E(y_i) = \sum_{j=1}^k w_{ij} f(x_{ij}; \boldsymbol{\beta}). \quad (6)$$

195 Under the linear model, this yields:

$$196 \quad E(y_i) = \sum_{j=1}^k w_{ij} [\beta^{(1)} + \beta^{(2)} x_{ij}] = \beta^{(1)} \sum_{j=1}^k w_{ij} + \beta^{(2)} \sum_{j=1}^k w_{ij} x_{ij}. \quad (7)$$

197 Assuming that x_{ij} have a resolution invariant mean (equation 2), this yields

$$198 \quad E(y_i) = \beta^{(1)} + \beta^{(2)} x_i, \quad (8)$$

199 which is exactly the same as the direct prediction at the cell level. Equations 7 and 8 generalize to
200 multiple linear models as well.

201 The additivity of the response variable is usually not achieved if nonlinear transformations are used in the
202 predictors. For example, $a_i \ln(y_i)$ is not equal to $\sum_{j=1}^{k_i} a_{ij} \ln(y_{ij})$. One might consider overcoming this
203 problem by using back-transformed predictions from a linear model of transformed y , but the right-hand
204 side of the prediction model would not be a linear function of predictors. In addition, the treatment of the
205 back-transformation bias of such models would be an additional issue in such an approach.

206 To summarize, resolution invariance in ABA is obtained at least when all of the following four conditions
207 are met:

208 Condition 1: ALS echoes are regularly spaced in the horizontal dimension

209 Condition 2: the forest variable (y) of interest is additive

210 Condition 3: the ALS-based metrics (x) have a resolution invariant mean

211 Condition 4: a linear model is used without nonlinear transformations in y

212 Condition 1 has not received much attention in the literature thus far because the literature on this topic
213 tends to deal with regularly spaced data. Condition 2 is not always satisfied because some inventory

214 attributes are not additive in nature. Commonly used metrics in ABA do not satisfy condition 3, but in
215 principle, some ABA metrics are satisfactory provided condition 1 is also satisfied. Condition 4 can be
216 satisfied, for example, with a classical linear regression model (Searle, 1971).

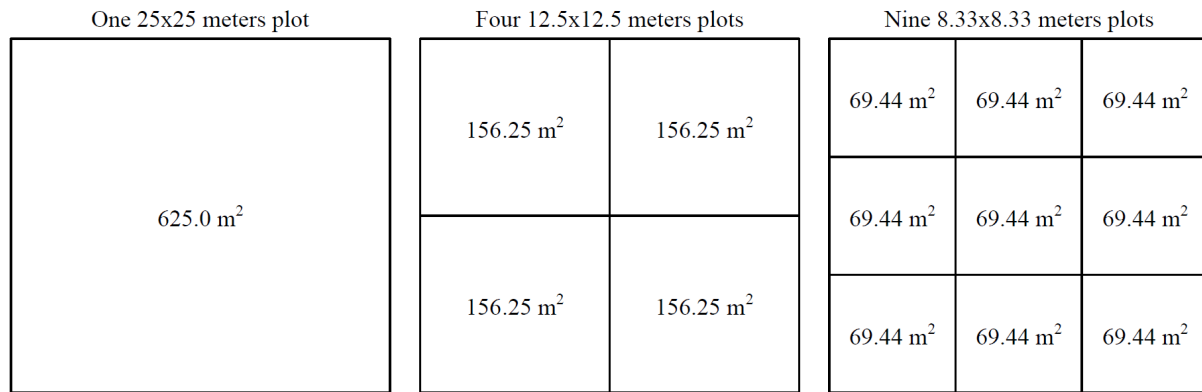
217 **Material**

218 *Field data*

219 The study area is a boreal managed forest area in eastern Finland (62°31'N, 30°10'E). Field
220 measurements were carried out in the summer of 2010 and sample plots were deliberately placed to
221 represent the tree size and species variation for the study area. The allocation of field plots was based on
222 the development stage of the forest and the dominant tree species. Scots pine (*Pinus sylvestris* L.) is the
223 dominant tree species representing about 75 % of the volume and the remainder consists of Norway
224 spruce (*Picea abies* [L.] Karst.) and a mixture of native deciduous species. We used field measurements
225 from 58 sample plots (25 x 25 m).

226 For trees with either a diameter at breast height (DBH) exceeding 4 cm or height exceeding 4 m, the
227 DBH, height, and tree species were recorded. The DBH of each tree was estimated as the average of the
228 maximum diameter and the diameter perpendicular to the maximum diameter. The above ground biomass
229 of the individual trees was calculated as a function of DBH and tree height using the species-specific
230 models developed by Repola (2008) and Repola (2009).

231 Each 25 x 25 m plot was divided into four 12.5 x 12.5 m plots and nine 8.33 x 8.33 m plots (Figure 1).
232 Delineation of sub-plot boundaries was feasible because the tree locations were known. For a more
233 detailed description of tree location determination see Packalen et al. (2015). In total, there were 58 25 x
234 25 m plots, 232 12.5 x 12.5 m plots and 522 8.33 x 8.33 m plots. Hereafter, we refer to these as 25.0 m,
235 12.5 m and 8.33 m resolutions. Plot level biomass per hectare (AGB Mg·ha⁻¹) for a plot (or a sub-plot)
236 was computed as the sum of tree biomass on a plot (or a sub-plot), expanded by the ratio of one hectare
237 over the plot area. A summary of AGB by plot size is provided in Table 1.



238

239 Figure 1. Plot setting.

240 Table1. Mean, standard deviation, minimum and maximum above ground biomass (AGB) by plot size.

	Plot size		
	8.33 m	12.5 m	25.0 m
Mean AGB ($\text{Mg}\cdot\text{ha}^{-1}$)	109.2	109.2	109.2
Std AGB ($\text{Mg}\cdot\text{ha}^{-1}$)	59.2	45.8	37.1
Min AGB ($\text{Mg}\cdot\text{ha}^{-1}$)	0.0	25.0	50.6
Max AGB ($\text{Mg}\cdot\text{ha}^{-1}$)	541.2	310.5	212.0

241 *ALS data*

242 ALS data were collected on June 26, 2009 using an Optech ALTM Gemini laser scanning system. The
 243 nominal pulse density was approximately 12 pulses per square meter. The test site was scanned from an
 244 altitude of approximately 600 m above ground level, with a field of view of 26 degrees and side overlap
 245 between transects of 55 %. Pulse repetition frequency was set to 125 kHz. A Digital Terrain Model
 246 (DTM) was constructed by first classifying points as ground and non-ground hits according to the
 247 approach described by Axelsson (2000). A raster DTM of 0.5 m spatial resolution was then obtained by
 248 interpolation using Delaunay triangulation. Heights above ground (dZ) for ALS echoes were calculated
 249 by differencing their elevations above the ellipsoid from corresponding DTM elevations. Hereafter, we
 250 refer to dZ as echo height.

251

252 **Methods**

253 *Predictor variables*

254 The ALS metrics used as predictor variables were computed in the same way for each plot at different
255 resolutions. The metrics were computed with either first or last echoes. First echoes contain original echo
256 categories “first of many” and “only” and last echoes contain “last of many” and “only”. Subscript f
257 denotes that a predictor variable was computed using a set of first echoes and correspondingly subscript l
258 denotes that last echoes were used. Regression models contain the following predictor variables:

- 259 • Height percentiles [$h5_f$, $h10_f$, $h20_f$, $h30_f$, $h40_f$, $h50_f$, $h60_f$, $h70_f$, $h80_f$, $h90_f$, $h95_f$ and $h95_l$] using
260 echoes with dZ at least 2 m. These variables do not have *resolution invariant means*.
- 261 • Mean height [$havg_f$] of echoes. This variable has a *resolution invariant mean* assuming the
262 number of echoes per plot is constant.
- 263 • Mean height [$havg_{f>2m}$] of echoes with dZ at least 2 m. This variable does not have a *resolution*
264 *invariant mean* except if the echo density above 2 m is constant, or the varying echo density is
265 taken into account in some other way (see LLS-RXN).
- 266 • Proportions of echoes below the fixed height thresholds of 2 m [$p2m_f$] and 10 m [$p10m_l$] in
267 relation to all echoes of the same echo category. For instance, if the total number of echoes of the
268 same echo category (e.g. first echoes) within a plot is 100 and 40 of these are below 2 m, then
269 $p2m_f$ is assigned a value of 0.4. These variables have *resolution invariant means* assuming the
270 number of echoes per plot is constant.
- 271 • Proportions of echoes below the varying height threshold of $havg_l$ [$pavg_l$] in relation to all echoes
272 of the same echo category. For instance, if the total number of echoes of the same echo category
273 (here last echoes) within a plot is 100 and 60 of these are below the height defined by $havg_l$ (e.g.
274 15 m), then $pavg_l$ is assigned a value of 0.6. This variable does not have a *resolution invariant*
275 *mean*.

276 Broadly similar predictor variables have been used in previous ABA studies and operational inventory
277 projects (see e.g. chapters 1, 11 and 12 in Maltamo et al. 2014).

278 *Model forms*

279 We formulated a set of regression models to reveal the effect of changing resolution. Plot level AGB was
280 the response variable in all the models. AGB is an additive response variable and no transformations were
281 carried out. Predictor variables and model forms were selected such that they represent a realistically wide
282 variety of model options in ABA. We examined two types of models; linear (LLS) and nonlinear (NLS).
283 Regression models contain two types of predictor variables; those that have resolution invariant mean
284 (XR) and those that have not (XNR). Note that the predictor variables categorized here as XR have the
285 property of a resolution invariant mean in the statistical sense but are not resolution invariant in the ABA
286 arena because of the non-regular pattern of ALS echoes and/or threshold value used to compute the
287 metric. The name of the equation depicts the type of model and predictors, for instance, LLS-XR denotes
288 that a model is linear and that the predictor variables have a resolution invariant mean.

289 $AGB = \beta_0 + \beta_1 \text{havg}_f + \beta_2 \text{p10m}_1 + \varepsilon$, (LLS-XR, 9)

290 $AGB = \beta_0 + \beta_1 \text{h95}_f + \beta_2 \text{pavg}_1 + \varepsilon$, (LLS-XNR, 10)

291 $AGB = \lambda e^{(\beta_0 + \beta_1 \text{havg}_f + \beta_2 \text{p2m}_1)} + \varepsilon$, (NLS-XR, 11)

292 $AGB = \lambda e^{(\beta_0 + \beta_1 \text{h95}_f + \beta_2 \text{pavg}_1)} + \varepsilon$, (NLS-XNR, 12)

293 where β_0, \dots, β_2 are coefficients to be estimated from data, ε the residual vector and λ that forces a zero
294 mean of residuals. When λ is omitted, the NLS-XR and NLS-XNR models provide a slightly non-zero
295 mean of residuals because there is no intercept in the selected model form. The calibration factor is used
296 for convenience because we require the NLS models to provide a zero mean of residuals when model
297 fitting and prediction are done at the same resolution.

298 In addition to the four models described above, we constructed a model that is entirely resolution
299 invariant. This model makes an implicit assumption that areas with a higher point density are more
300 important than areas with a low point density. This cannot be avoided if resolution invariance is desired
301 and metrics are computed directly from ALS echoes. Resolution invariance is obtained by taking into

302 account the varying number of echoes per unit of area while computing predictor variables. The model
 303 resembles the LLS-XR except that the mean height of ALS echoes was computed from above 2 m echoes.
 304 The predictor variable $\text{havg}_{f>2m}$ was rescaled as follows:

$$305 \quad \Omega(\text{havg}_f) = n_{f>2m} \text{havg}_{f>2m} , \quad (13)$$

306 where $n_{f>2m}$ is the number of first echoes having dZ at least 2 m per area unit (e.g. per square meter) in
 307 a plot or subplot. The predictor variable $p10m_l$ was rescaled as follows:

$$308 \quad \Omega(p10m_l) = n_l p10m_l , \quad (14)$$

309 where n_l is the number of last echoes per unit area in a plot or subplot. Note that rescaling is always
 310 conducted using the number of echoes that are used to compute the metric in question, i.e. height
 311 threshold must be taken into account if applied before computing a metric. Thus, the resolution invariant
 312 model is as follows:

$$313 \quad AGB = \beta_0 + \beta_1 \Omega(\text{havg}_{f>2m}) + \beta_2 \Omega(p10m_l) + \varepsilon , \quad (\text{LLS-RXN}, 15)$$

314 where RXN denotes that XN type predictor variables were rescaled. We also fitted a set of HPERC
 315 models to demonstrate the bias properties for the commonly used predictor variable $h[5\dots95]_f$ (height
 316 percentile computed by excluding echoes near to the ground) when combined with another common
 317 predictor $p2m_f$ (proportion of echoes below 2 m). HPERC models have the form:

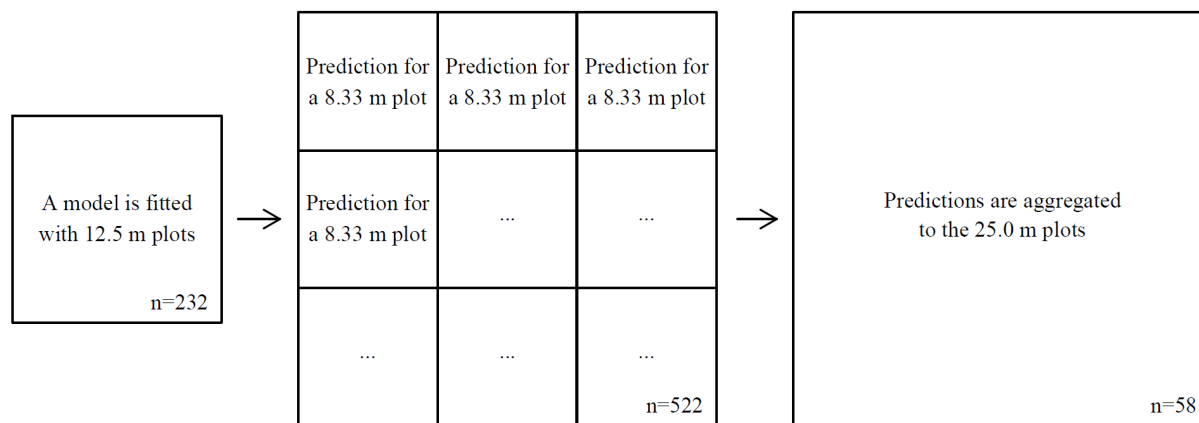
$$318 \quad AGB = \beta_0 + \beta_1 p2m_f + \beta_2 h[5\dots95]_f + \varepsilon , \quad (\text{HPERC}, 16)$$

319 where height percentile varies between 5 and 95. The model form was selected such that it fits well with
 320 all the percentiles.

321 *Model fitting, prediction and validation*

322 We fitted the models at the resolutions of 8.33 m, 12.5 m and 25.0 m with the method of least squares
 323 using *lm* and *nls* functions available in the R environment (R Development Core Team 2011). Then we

324 predicted at all resolutions with every model. The performance of models was assessed by cross-
 325 validation. First, one 25 m plot was excluded and a model was fitted with other plots either at 8.33 m,
 326 12.5 m or 25.0 m resolution. Then the prediction was made to the excluded 25 m plot, either at 8.33 m,
 327 12.5 m or 25.0 m resolution. Thus, each model was fitted three times ($\times 58$ considering cross-validation)
 328 and was then used to predict at its native resolution and two other resolutions. This was repeated with
 329 models that violate the resolution invariance conditions (LLS-XR, LLS-XNR, NLS-XR, NLS-XNR) and,
 330 as a *proof-of-concept*, with the proposed resolution invariant model (LLS-RXN). All the predictions were
 331 aggregated to the 25.0 m level by computing the mean value of sub-plots. The example in Figure 2
 332 describes a model that is first fitted at the 12.5 m resolution, then used to predict at the 8.33 m resolution,
 333 and finally predictions are aggregated to the 25.0 m resolution. This setting enables an analysis of
 334 resolution effect when a plot size is either smaller or bigger in model fitting than in prediction.



335
 336 Figure 2. An example of model fitting, prediction and aggregation workflow. For the simplicity, cross-
 337 validation is not shown in the figure.

338 The purpose of HPERC models is to demonstrate the bias properties for the commonly used predictor
 339 variable $h[5\dots95]_f$ when combined with another common predictor $p2m_f$. This was done by fitting
 340 HPERC models at resolutions of 8.33 m and 25.0 m. For each height percentile, the 8.33 m model was
 341 used to directly predict at a resolution of 25.0 m, whereas the 25.0 m model was used to predict to a
 342 resolution of 8.33 m and the predictions were then aggregated to the 25.0 m resolution.

343 We assess the performance at the 25.0 m resolution using the estimated relative BIAS and RMSE.

344
$$\text{RMSE-}\% = 100 \times \frac{\sqrt{\frac{\sum_{i=1}^n (\hat{y}_i - y_i)^2}{n}}}{\bar{y}}, \quad (17)$$

345
$$\text{BIAS-}\% = 100 \times \frac{\frac{\sum_{i=1}^n (\hat{y}_i - y_i)}{n}}{\bar{y}}, \quad (18)$$

346 where \hat{y}_i is the predicted value in plot i , y_i is the observed value in plot i , n is the number of plots, and \bar{y}
 347 is the mean of observed values.

348 **Results**

349 *Error rate*

350 The RMSE values and the change of RMSE compared to its value in native resolution are presented in
 351 Table 2. The RMSE decreased if the prediction resolution was higher than the fitting resolution, and
 352 conversely, the RMSE increased if the prediction resolution was lower than the fitting resolution. This
 353 trend was obvious but not consistent in every case. The effect of varying resolution was slightly stronger
 354 when fitting at high resolution and predicting at low resolution than vice versa. In most cases, the lowest
 355 error rate was obtained when a model was fitted at the largest resolution and prediction was carried out at
 356 the finest resolution. The resolution effect tended to be much smaller with predictor variables that had a
 357 resolution invariant mean (LLS-XR and NLS-XR) than with variables that did not have this property
 358 (LLS-XNR and NLS-XNR). The model type (LLS or NLS) did not have any apparent effect. The
 359 resolution invariant LSS-RXN model had a constant RMSE value under different resolution predictions
 360 when the regression coefficients were fixed (i.e. they are solved at a certain resolution). This was due to
 361 the exact same predictions at different resolutions. In this instance too, the error rate decreased as the
 362 fitting resolution became lower. The RMSE values ranged from 16.74 to 20.73 %.

363 Table 2. RMSE values (%) for the different models and resolutions. Fitting resolution is by rows and
 364 prediction resolution by columns. The change of RMSE compared to its value in native resolution
 365 (diagonal) is shown in parenthesis. Absolute RMSE values ($\text{Mg}\cdot\text{ha}^{-1}$) are in appendix A1.

Predict

Model		Plot size	8.33 m	12.5 m	25.0 m
LLS-XR	Fit	8.33 m	17.38 (0.00)	17.54 (0.16)	17.53 (0.15)
		12.5 m	16.81 (-0.10)	16.91 (0.00)	16.91 (0.00)
		25.0 m	16.74 (-0.05)	16.80 (0.01)	16.79 (0.00)
LLS-XNR	Fit	8.33 m	19.90 (0.00)	20.46 (0.56)	20.73 (0.82)
		12.5 m	19.01 (-0.34)	19.35 (0.00)	19.50 (0.15)
		25.0 m	19.18 (-0.21)	19.35 (-0.04)	19.39 (0.00)
NLS-XR	Fit	8.33 m	18.37 (0.00)	18.32 (-0.05)	18.40 (0.03)
		12.5 m	17.49 (-0.03)	17.52 (0.00)	17.58 (0.06)
		25.0 m	17.24 (-0.10)	17.28 (-0.06)	17.34 (0.00)
NLS-XNR	Fit	8.33 m	19.01 (0.00)	19.98 (0.97)	20.25 (1.24)
		12.5 m	18.07 (-0.57)	18.64 (0.00)	18.67 (0.03)
		25.0 m	18.27 (-0.33)	18.63 (0.02)	18.61 (0.00)
LLS-RXN	Fit	8.33 m	17.77 (0.00)	17.77 -(0.00)	17.77 (0.00)
		12.5 m	17.75 (0.00)	17.75 -(0.00)	17.75 (0.00)
		25.0 m	17.68 (0.00)	17.68 (0.00)	17.68 (0.00)

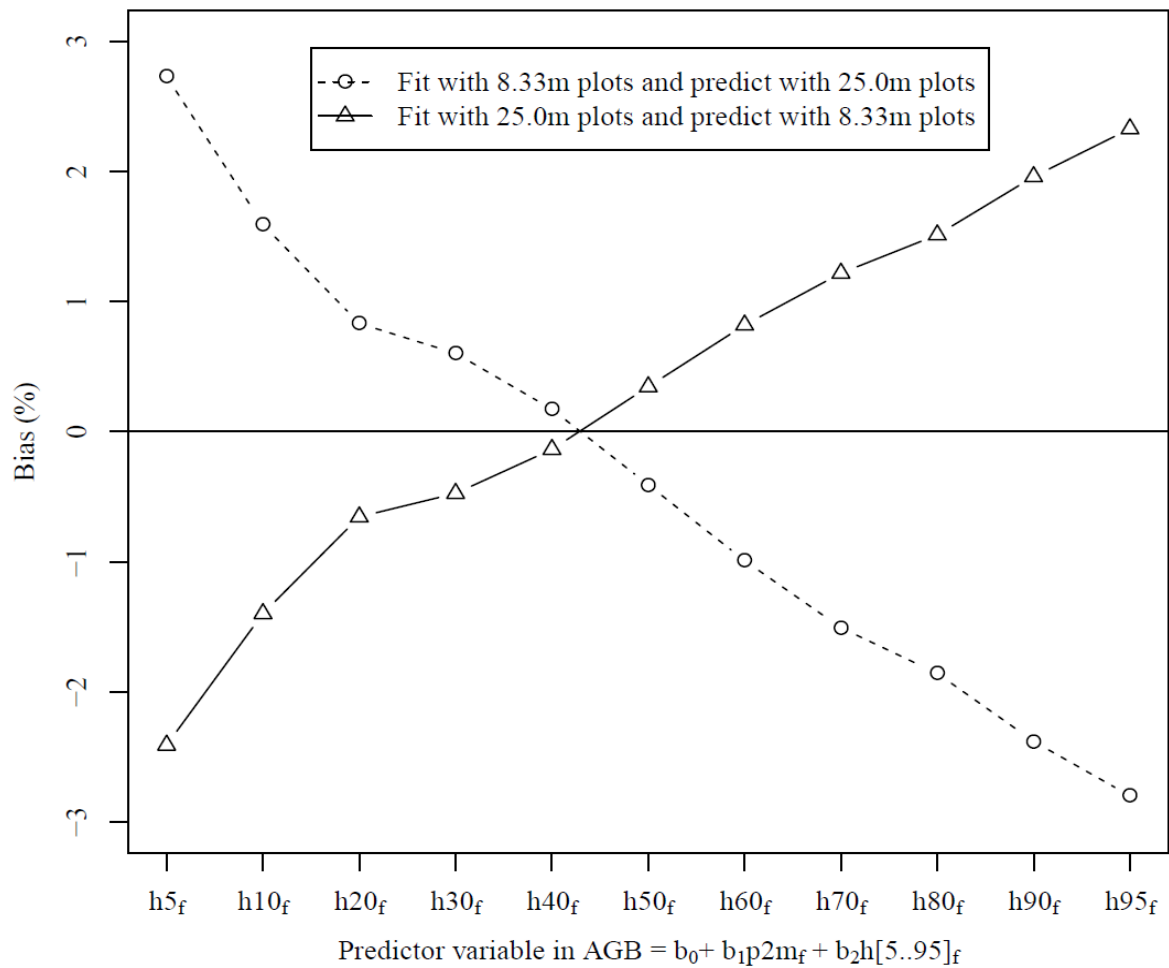
366 *Bias*

367 The BIAS values for the different models and resolutions are presented in Table 3. The resolution effect
368 with respect to BIAS was smaller with predictor variables that had a resolution invariant mean (LLS-XR
369 and NLS-XR) than with variables that did not have this property (LLS-XNR and NLS-XNR). If the
370 prediction resolution was lower than the fitting resolution it resulted in an overestimation, and conversely,
371 if the prediction resolution was higher than the fitting resolution it produced an underestimation.
372 However, the direction of BIAS was different in NLS-XR than in the other cases. There was no clear
373 difference in terms of BIAS between the linear (LLS) and non-linear (LLS) models. The LLS-RXN
374 models showed small BIAS, which was consistent with the same model at different resolutions. This
375 small BIAS is due to cross-validation; without cross-validation the LLS-RXN models show zero BIAS.

376 Table 3. BIAS values (%) for the different models and resolutions. Fitting resolution is by rows and
 377 prediction resolution by columns. Negative values denote an underestimation and positive values an
 378 overestimation (eq. 18). Absolute RMSE values ($\text{Mg}\cdot\text{ha}^{-1}$) are in appendix A2.

Model		Plot size	Predict		
			8.33 m	12.5 m	25.0 m
LLS-XR	Fit	8.33 m	-0.03	0.12	0.21
		12.5 m	-0.16	-0.02	0.07
		25.0 m	-0.21	-0.09	-0.01
LLS-XNR	Fit	8.33 m	-0.03	1.46	3.03
		12.5 m	-1.36	0.00	1.45
		25.0 m	-2.60	-1.35	0.01
NLS-XR	Fit	8.33 m	-0.02	-0.71	-1.48
		12.5 m	0.56	0.05	-0.55
		25.0 m	0.97	0.55	0.05
NLS-XNR	Fit	8.33 m	-0.02	1.50	2.61
		12.5 m	-1.32	0.06	1.08
		25.0 m	-2.26	-0.94	0.07
LLS-RXN	Fit	8.33 m	-0.13	-0.13	-0.13
		12.5 m	-0.11	-0.11	-0.11
		25.0 m	-0.12	-0.12	-0.12

379 Figure 3 shows the effect of using varying height percentile on prediction BIAS (HPERC models). A
 380 clear trend in the opposing directions was observed. Fitting with the 8.33 m resolution and predicting with
 381 the 25.0 m resolution led to a positive BIAS with low percentiles and a negative BIAS with high
 382 percentiles, while fitting with the 25.0 m resolution and predicting with the 8.33 m resolution led to a
 383 negative BIAS with low percentiles and positive BIAS with high percentiles. The more extreme the
 384 percentile, the more serious the BIAS; the highest BIAS was 2.8%. We can interpolate between the nodes
 385 in the graph and estimate that (in this case) unbiased predictions could be obtained with the 43th
 386 percentile.



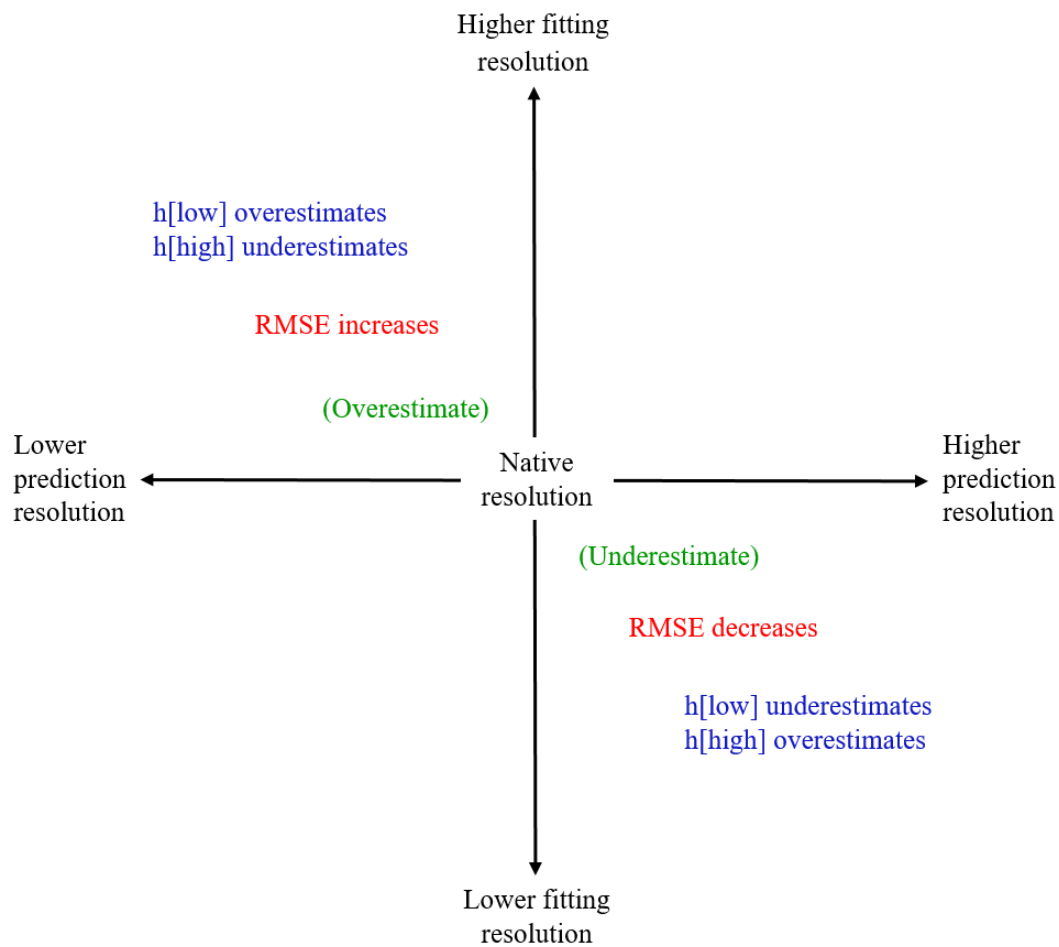
387

388 Figure 3. Behavior of BIAS using fixed p_{2m_f} variable and varying height percentile $h[5..95]_f$ (HPERC
 389 models). Line -○- depicts the case where a model is fitted at the resolution of 8.33 m and the prediction is
 390 done at the resolution of 25.0 m. Line -△- depicts the opposite; a model is fitted at the 25.0 m resolution
 391 and the prediction is done at the 8.33 m resolution.

392 **Discussion**

393 The main findings of the behavior of RMSE and BIAS with respect to differing fitting and prediction
 394 resolutions are summarized in Figure 4. The RMSE value increases when the prediction resolution is
 395 lower than the fitting resolution and decreases when the fitting resolution is lower than the prediction
 396 resolution. The direction of BIAS was not consistent across all models. In most cases, however, the result
 397 was an overestimation when the prediction resolution was lower than the fitting resolution, and vice
 398 versa. This indicates that the direction of BIAS also depends on the model form. Predicting at resolutions

399 lower than the fitting resolution leads to an overestimation with low height percentiles ($h[\text{low}]$) and an
 400 underestimation with high height percentiles ($h[\text{high}]$), while predicting at resolutions higher than the
 401 fitting resolution leads to an underestimation with low percentiles and an overestimation with high
 402 percentiles. This is due to the bias of sample percentiles as estimators of population percentiles. The
 403 sample percentiles overestimate low population percentiles and underestimate the high percentiles
 404 (Hyndman and Fan, 1996).



405

406 Figure 4. Main findings of the study with respect to lower vs. higher fitting and prediction resolutions.
 407 Overestimate and underestimate in brackets denotes that the direction of BIAS was not consistent across
 408 all models, but in most cases it was as depicted. $h[\text{low}]$ and $h[\text{high}]$ refer to low and high height
 409 percentiles, respectively.

410 Our results indicate that the lowest error rate is obtained when a model is fitted at the lowest resolution
411 and when prediction is done at the highest resolution. A reason for this may be that the metrics computed
412 from larger plots lead to regression coefficients that are closer to the true value than those obtained with
413 small plot sizes. This may be due to larger measurement errors in predictions that use smaller plots
414 (Gobakken and Næsset, 1999), which reduce regression coefficient estimates towards zero (Lappi, 1993;
415 Carroll et al., 2006), or because the edge tree effect, which is similar to a measurement error, is greater in
416 the smaller plots (Packalen et al., 2015). However, as there is a tradeoff between plot size and the number
417 of plots it is not obvious which plot size is optimal given the need for sufficient numbers of plots as well
418 as sufficiently large plots. In the real world, resources available for field measurements are typically
419 limited, and increasing the plot areas would result in a fewer numbers of plots.

420 The level of BIAS in this study seems to be quite low even if several conditions of resolution invariance
421 are violated at the same time. The maximum bias of 3.03 % is observed when the resolution is changed 9-
422 fold. When the resolution is changed 4-fold, the maximum bias is 1.50 %. In a real world scenario, the
423 change of resolution is hardly ever as high as 4-fold. The effect of resolution on BIAS is smaller with
424 predictor variables that have a resolution invariant mean than with variables that do not have this
425 property. In the case of the linear model and predictor variables with a resolution invariant mean (LLS-
426 XR), the maximum bias is only 0.21 % when the resolution is changed 9-fold. However, it should be
427 noted that it is not exactly a resolution invariant because the number of ALS points per cell varies.

428 The Pearson correlation coefficient between the BIAS (Table 3) and change of RMSE (Table 2, figures in
429 parenthesis) is 0.78 when all 54 cases are considered. This is expected behavior because $RMSE^2 = BIAS^2$
430 + variance. There is a trend that BIAS is positive when RMSE increases with respect to the native
431 resolution, and vice versa when it decreases. The NLS-XR model was an exception: underestimation
432 increased and overestimation decreased RMSE with respect to the native resolution. We can conclude that
433 the decrease or increase of RMSE values with respect to native resolution does not depend on the sign of
434 BIAS but depends on model form and predictor variables.

435 Resolution invariant prediction is feasible with LLS-RXN. The main idea is to rescale predictor variables
436 in order to take into account the varying number of echoes per unit of area (eq. 13-14). Otherwise, LLS-
437 RXN is the same as LLS-XR. “Resolution invariance” means that prediction BIAS is always exactly zero,
438 although there is a tradeoff in terms of RMSE. LLS-RXN has consistently higher RMSE values than
439 LLS-XR, because the weighting does not contribute to the relationship between response and predictor
440 values – they simply enforce a desired condition of resolution invariance. Therefore, a greater RMSE is
441 the price to be paid for exact resolution invariance. It is also debatable whether weighting with the
442 number of echoes per unit area makes sense. LLS-RXN corrects for the effects of irregular point density
443 resulting from variability in the ALS data acquisition process. Consequently, areas with a higher point
444 density receive higher weighting than areas with lower point density – where in practice, we are equally
445 interested in every location. An alternative approach to revise irregular point density would be to
446 standardize ALS point density per area unit by interpolating a continuous surface and computing metrics
447 from this surface, instead of computing them directly from the ALS echoes. A canopy height model
448 (CHM) is an example of this kind of surface: condition 1 is fulfilled if plots and cells are arranged such
449 that the number of pixels per unit area is the same in every plot and cell. Zhao et al. (2009) used this
450 approach to derive canopy height distributions. Chirici et al. (2016) studied the decrease in accuracy if
451 CHM metrics are used instead of echo metrics in the estimation of forest aboveground biomass. They
452 found that the R^2 decreased from 0.58 to 0.56 with a linear model, and from 0.54 to 0.48 with the k-NN
453 technique. Undoubtedly, the use CHM metrics increases the prediction error but this trade-off may be
454 acceptable. On the other hand, if unbiasedness is not a strict requirement, the effect of a slight imbalance
455 in the number of echoes per unit area may not have very much practical significance.

456 Note that the LLS-RXN model accounts for the effect of varying point density both within and between
457 plots (and cells). In classical ABA, between plots (or cells) variation in point density is not an issue
458 because the value of metrics do not depend on the number of points per plot. However, an intrinsic
459 property of the classical ABA is that higher point density areas within a plot get more weight than lower

460 point density areas within a plot. The use of a continuous surface, such as computing metrics from the
461 CHM, does not have an issue with either within a plot or between plots variation in point density.

462 It is possible to use only ALS metrics that fulfill the condition of a resolution invariant mean, but there
463 are several commonly used metrics that do not obey this condition. Height percentile is the most common
464 category of this type and is frequently used because there is a strong relationship between upper
465 percentiles and the main attributes of interest in forest inventories (Næsset, 2002). It is also common
466 practice to include only vegetation echoes when computing height metrics. Typically, this is implemented
467 by excluding echoes below 1-2 m (Næsset, 2004; Vauhkonen et al., 2012; Chen et al., 2016). The
468 application of a height threshold makes the situation even more difficult from a resolution viewpoint,
469 because it causes the number of echoes considered by a metric to vary considerable cell by cell. Figure 3
470 demonstrates the behavior of BIAS with a linear model mimicking a real world use case when the
471 resolution is changed 9-fold. The model contains one cover metric and varying height percentiles 5...95
472 computed with a height threshold of 2 m. This shows that bias increases more or less symmetrically
473 towards the extreme percentiles. If resolution bias is of concern, then it can be mitigated to some degree
474 by simply avoiding extreme percentiles.

475 Drawing absolute conclusions with regard to the level of BIAS or RMSE is difficult when resolution
476 invariance conditions are not met and the resolution is changed. For example, one may use a non-linear
477 model form that is exceedingly sensitive to resolution, or a predictor variable that may be extremely
478 sensitive to resolution, such as maximum echo height. In cases when forest inventory attributes that are
479 not additive in nature, such as Lorey's Height (mean height weighted by basal area) or DGM (diameter of
480 the basal area median tree), resolution invariance cannot be achieved with the methods examined here,
481 and the observations made here with regard to BIAS and RMSE do not apply.

482 The use of 3D remote sensing data is becoming increasingly widespread and different point cloud
483 generation approaches are now available. Point cloud reconstruction from image pairs is currently the
484 most common alternative (St-Onge et al., 2008) to ALS and also new Lidar techniques have emerged

485 (Swatantran et al., 2016). The observations made in this study apply partly to image point clouds but there
486 are differences that must be taken into account. For example, some image point cloud software produces a
487 regularly spaced surface model instead of a true point cloud, in which case varying point density is not an
488 issue.

489 **Conclusions**

490 A number of factors contribute to resolution dependence in ABA forest inventories. These include the
491 varying point density of the ALS data, the type of response variable used, how the predictor variables are
492 computed, and the properties of the model. Complete resolution invariance is feasible using the LLS-
493 RXN approach, or by computing metrics from a continuous surface interpolated with ALS data (i.e.
494 CHM) and by meeting other conditions too.

495 The maximum BIAS was 1.50 % and the maximum change of RMSE compared to its value in native
496 resolution was 0.97 % when there was a 4-fold difference in resolution. This indicates that the resolution
497 effect is small in most real-world use cases, especially as the difference in plot or cell size is usually
498 considerably smaller than the 4-fold. The effect of resolution on BIAS and change of RMSE compared to
499 its value in native resolution was much smaller with XR than XNR type metrics. Therefore, if resolution
500 effect is of concern, XR type metrics are recommended, although they are not resolution invariant in an
501 ABA context because the number of ALS echoes per unit area is not constant. In this study, the model
502 type (LLS or NLS) did not have any clear effect on BIAS or change of RMSE.

503 Unbiasedness is not a strict requirement in most stand level forest management inventories. In that case,
504 resolution invariance may be of limited practical importance, particularly because at the stand level the
505 error rate will typically greatly exceed the level of bias caused by the resolution invariance. For strategic
506 inventories that cover large areas, the importance of resolution invariance is greater. In a model-based or
507 model-assisted approach to estimation over large areas, it is assumed that model residuals are an unbiased
508 sample of the deviations that would be observed between predictions and observations. In the case of
509 resolution differences between the fitting and prediction datasets, this property does not hold, and the bias

510 may be large relative to the sampling variation. Attention to resolution dependence will thus be most
511 relevant when large area inferences are made from ALS-assisted inventories.

512 **References**

513 Axelsson, P., 2000. DEM generation from laser scanner data using adaptive TIN models. In: International
514 Archives of Photogrammetry and Remote Sensing, Amsterdam, The Netherlands, 16–22 July 2000, Vol.
515 XXXIII, part B4, 110–117.

516 Carroll, R.J., Ruppert, D., Stefanski, L.A., Crainiceanu, C.M., 2006. Measurement Error in Nonlinear
517 Models: A Modern Perspective (Second ed.). Chapman and Hall/CRC (484 p).

518 Chasmer, L., Barr, A., Hopkinson, C., McCaughey, H., Treitz, P., Black, A., Shashkov, A., 2009. Scaling
519 and assessment of GPP from MODIS using a combination of airborne lidar and eddy covariance
520 measurements over jack pine forests. *Remote Sensing of Environment* 113, 82–93.

521 Chen, Q., McRoberts, R.E., Wang, C., Radtke, P.J., 2016. Forest aboveground biomass mapping and
522 estimation across multiple spatial scales using model-based inference. *Remote Sensing of Environment*
523 184, 350–360.

524 Chirici, G., McRoberts, R.E., Fattorini, L., Mura, M., Marchetti, M., 2016. Comparing echo-based and
525 canopy height model-based metrics for enhancing estimation of forest aboveground biomass in a model-
526 assisted framework. *Remote Sensing of Environment* 174, 1–9.

527 Frazer, G.W., Magnussen, S., Wulder, M.A., Niemann, K.O., 2011. Simulated impact of sample plot size
528 and co-registration error on the accuracy and uncertainty of LiDAR-derived estimates of forest stand
529 biomass. *Remote Sensing of Environment* 115, 636-649.

530 Gobakken, T., Næsset, E. 2009. Assessing effects of positioning errors and sample plot size on
531 biophysical stand properties derived from airborne laser scanner data. *Canadian Journal of Forest*
532 *Research* 39, 1036-1052.

533 Goetz, S., Dubayah, R., 2011. Advances in remote sensing technology and implications for measuring
534 and monitoring forest carbon stocks and change. *Carbon Management* 2:3, 231–244.

535 Grafström, A., Zhao, X., Nylander, M., Petersson, H., 2017. A new sampling strategy for forest
536 inventories applied to the temporary clusters of the Swedish national forest inventory. *Canadian Journal*
537 *of Forest Research* 47, 1161–1167.

538 Gregoire, T.G., Næsset, E., McRoberts, R.E., Ståhl, G., Andersen, H.-E., Gobakken, T., Ene, L., Nelson,
539 R., 2016. Statistical rigor in LiDAR-assisted estimation of aboveground forest biomass. *Remote Sensing*
540 *of Environment* 173, 98–108.

541 Hudak, A.T., Crookston, N.L., Evans, J.S., Hall, D.E., Falkowski, M.J., 2008. Nearest neighbor
542 imputation of species-level, plot-scale forest structure attributes from LiDAR data. *Remote Sensing of*
543 *Environment* 112, 2232–2245.

544 Hyndman, R. J., Fan, Y., 1996. Sample quantiles in statistical packages. *American Statistician* 50, 361–
545 365.

546 Hyypä, J., Hyypä, H., Leckie, D., Gougeon, F., Yu, X., Maltamo, M., 2008. Review of methods of
547 small-footprint airborne laser scanning for extracting forest inventory data in boreal forests. *International*
548 *Journal of Remote Sensing* 29, 1339–1366.

549 Hyypä, J., Kelle, O., Lehtikoinen, M., Inkinen, M., 2001. A segmentation-based method to retrieve stem
550 volume estimates from 3-D tree height models produced by laser scanners. *IEEE Transactions on*
551 *Geoscience and Remote Sensing* 39, 969-975.

552 Junttila, V., Finley, A.O., Bradford, J.B., Kauranne, T., 2013. Strategies for minimizing sample size for
553 use in airborne LiDAR-based forest inventory. *Forest Ecology and Management* 292, 75–85.

554 Keränen, J., Maltamo, M., Packalen, P., 2016. Effect of flying altitude, scanning angle and scanning mode
555 on the accuracy of ALS based forest inventory. *International Journal of Applied Earth Observation and*
556 *Geoinformation* 52, 349–360.

557 Koch, B., Heyder, U., Weinacker, H., 2006. Detection of individual tree crowns in airborne lidar data.
558 *Photogrammetric Engineering & Remote Sensing* 72, 357–363.

559 Lähivaara, T., Seppänen, A., Kaipio, J.P., Vauhkonen, J., Korhonen, L., Tokola, T., Maltamo, M., 2014.
560 Bayesian approach to tree detection based on airborne laser scanning data. *IEEE Transactions on*
561 *Geoscience and Remote Sensing* 52, 2690–2699.

562 Lappi, J., 1993. *Metsäbiometrian menetelmiä*. *Silva Carelica* 24. University of Joensuu (182 p).

563 Liang, S., 2004. *Quantitative Remote Sensing of Land Surfaces*. John Wiley & sons, Inc. Hoboken, New
564 Jersey (560 p).

565 Magnussen, S., Næsset, E., Gobakken, T., 2013. Prediction of tree-size distributions and inventory
566 variables from cumulants of canopy height distributions. *Forestry* 86, 583–595.

567 Maltamo, M., Næsset, E., Vauhkonen, J. 2014. *Forestry applications of airborne laser scanning -concepts*
568 *and case studies*. *Managing Forest Ecosystems* 27. Springer (464 p).

569 Marceau, D.J., Hay, G.J., 1999. Remote Sensing Contributions to the Scale Issue. *Canadian Journal of*
570 *Remote Sensing* 25, 357–366.

571 Means, J.E., Acker, S.A., Fitt, B.J., Renslow, M., Emerson, L., Hendrix, C.J., 2000. Predicting forest
572 stand characteristics with airborne scanning LiDAR. *Photogrammetric Engineering & Remote Sensing*
573 66, 1367–1372.

574 Næsset, E., 2002. Predicting forest stand characteristics with airborne scanning laser using a practical
575 two-stage procedure and field data. *Remote Sensing of Environment* 80, 88–99.

576 Næsset, E., 2004. Practical large-scale forest stand inventory using a small-footprint airborne scanning
577 laser. *Scandinavian Journal of Forest Research* 19, 164–179.

578 Næsset, E., 2005. Assessing sensor effects and effects of leaf-off and leaf-on canopy conditions on
579 biophysical stand properties derived from small-footprint airborne laser data. *Remote Sensing of*
580 *Environment* 98, 356–370.

581 Nilsson, M., Nordkvist, K., Jonzén, J., Lindgren, N., Axensten, P., Wallerman, J., Egberth, M., Larsson,
582 S., Nilsson, L., Eriksson, J., Olsson, H., 2017. A nationwide forest attribute map of Sweden predicted
583 using airborne laser scanning data and field data from the National Forest Inventory. *Remote Sensing of*
584 *Environment* 194, 447–454.

585 Niska, H., Skön, J-P., Packalén, P., Tokola, T., Maltamo, M., Kolehmainen, M., 2010. Neural Networks
586 for the Prediction of Species-Specific Plot Volumes Using Airborne Laser Scanning and Aerial
587 Photographs. *IEEE Transactions on Geoscience and Remote Sensing* 48, 1076–1085.

588 Packalén, P., Maltamo, M., 2007. The k-MSN method for the prediction of species-specific stand
589 attributes using airborne laser scanning and aerial photographs. *Remote Sensing of Environment* 109,
590 328–341.

591 Packalén, P., Mehtätalo, L., Maltamo, M., 2011. ALS-based estimation of plot volume and site index in a
592 eucalyptus plantation with a nonlinear mixed-effect model that accounts for the clone effect. *Annals of*
593 *Forest Science* 68, 1085–1092.

594 Packalen, P., Strunk, J., Pitkänen, J., Temesgen, H., Maltamo, M., 2015. Edge-tree Correction for
595 Predicting Forest Inventory Attributes Using Area-based Approach With Airborne Laser Scanning. *IEEE*
596 *Journal of Selected Topics in Applied Earth Observations and Remote Sensing* 8, 1274–1280.

597 R Development Core Team, 2011. R: A language and environment for statistical computing. R
598 Foundation for Statistical Computing, Vienna, Austria. ISBN 3-900051-07-0, URL [http://www.R-](http://www.R-project.org/)
599 [project.org/](http://www.R-project.org/).

600 Raffy, M., 1992. Change of scale in models of remote sensing: A general method for spatialization of
601 models. *Remote Sensing of Environment* 40, 101–112.

602 Reiss, R.-D., 1989. Approximate distributions of order statistics with applications to nonparametric
603 statistics. Springer-Verlag (355 p).

604 Repola, J., 2008. Biomass equations for birch in Finland. *Silva Fennica* 42, 605–624.

605 Repola, J., 2009. Biomass equations for Scots pine and Norway spruce in Finland. *Silva Fennica* 43, 625–
606 647.

607 Ruiz, A.L., Hermosilla, T., Mauro, F., Godino, M., 2014. Analysis of the Influence of Plot Size and
608 LiDAR Density on Forest Structure Attribute Estimates. *Forests* 5(5), 936–951.

609 Searle, S.R., 1971. *Linear models*. John Wiley & Sons, New York (532 p).

610 Simic, A., Chen, J.M., Liu, J., Csillag, F., 2004. Spatial scaling of net primary productivity using subpixel
611 information. *Remote Sensing of Environment* 93, 246–258.

612 St-Onge, B., Vega, C., Fournier, R.A., Hu, Y., 2008. Mapping canopy height using a combination of
613 digital stereo-photogrammetry and lidar. *International Journal of Remote Sensing* 29, 3343–3364.

614 Strahler, A.H., Woodcock, C.E., Smith, J.A., 1986. On the nature of models in remote sensing. *Remote*
615 *Sensing of Environment* 20, 121–139.

616 Strunk, J.L., Reutebuch, S.E., Andersen, H.-E., Gould, P.J., McGaughey, R., 2012. Model-assisted forest
617 yield estimation with light detection and ranging. *Western Journal of Applied Forestry* 27, 53–59.

618 Swatantran, A., Tang, H., Barrett, T., DeCola, P., Dubayah, R., 2016. Rapid, High-Resolution Forest
619 Structure and Terrain Mapping over Large Areas using Single Photon Lidar. *Scientific Reports* 6, Article
620 number: 28277.

621 Thomas, V., Treitz, P., McCaughey, J.H., Morrison I., 2006. Mapping stand-level forest biophysical
622 variables for a mixedwood boreal forest using lidar: an examination of scanning density, *Canadian*
623 *Journal of Forest Research* 36, 34–47.

624 Turner, M. G., Dale, V. H., Gardner, R. H., 1989. Predicting across scales: Theory development and
625 testing. *Landscape Ecology* 3, 245–252.

626 Vauhkonen, J., Seppänen, A., Packalén, P., Tokola, T., 2012. Improving species-specific plot volume
627 estimates based on airborne laser scanning and image data using alpha shape metrics and balanced field
628 data. *Remote Sensing of Environment* 124, 534–541.

629 Wu, H., Li, Z-L., 2009. Scale Issues in Remote Sensing: A Review on Analysis, Processing and
630 Modeling. *Sensors* 9, 1768–1793.

631 Zhao, K., Popescu, S.C., Nelson, R.F., 2009. Lidar remote sensing of forest biomass: A scale-invariant
632 estimation approach using airborne lasers. *Remote Sensing of Environment* 113, 182–196.

633

634

635

636

637

638

639

640

641

642

643

644

645 **List of Figure Captions**

646 Figure 1. Plot setting.

647 Figure 2. An example of model fitting, prediction and aggregation workflow.

648 Figure 3. Behavior of BIAS using fixed $p2m_f$ variable and varying height percentile $h[5 \dots 95]_f$ (HPERC
649 models).

650 Figure 4. Main findings of the study with respect to lower vs. higher fitting and prediction resolutions.

651 Overestimate and underestimate in brackets denotes that the direction of BIAS was not consistent across
652 all models, but in most cases it was as depicted. $h[\text{low}]$ and $h[\text{high}]$ refer to low and high height
653 percentiles, respectively.

654

655

656

657

658

659

660

661

662

663 Appendix A.

664 Table A1

665 Absolute RMSE values ($\text{Mg}\cdot\text{ha}^{-1}$) for the different models and resolutions. Fitting resolution is by rows
666 and prediction resolution by columns. The change of RMSE compared to its value in native resolution
667 (diagonal) is shown in parenthesis.

Model	Plot size	Predict		
		8.33 m	12.5 m	25.0 m
LLS-XR	8.33 m	18.98 (0.00)	19.16 (0.17)	19.15 (0.17)
	12.5 m	18.35 (-0.11)	18.47 (0.00)	18.46 (0.02)
	25.0 m	18.28 (-0.06)	18.35 (0.01)	18.34 (0.00)
LLS-XNR	8.33 m	21.74 (0.00)	22.34 (0.61)	22.63 (0.90)
	12.5 m	20.76 (-0.37)	21.13 (0.00)	21.30 (0.17)
	25.0 m	20.94 (-0.23)	21.13 (-0.04)	21.17 (0.00)
NLS-XR	8.33 m	20.06 (0.00)	20.01 (-0.06)	20.10 (0.03)
	12.5 m	19.10 (-0.03)	19.13 (0.00)	19.19 (0.06)
	25.0 m	18.83 (-0.11)	18.87 (-0.07)	18.94 (0.00)
NLS-XNR	8.33 m	20.76 (0.00)	21.82 (1.06)	22.11 (1.35)
	12.5 m	19.73 (-0.62)	20.35 (0.00)	20.39 (0.04)
	25.0 m	19.95 (-0.36)	20.34 (0.02)	20.32 (0.00)
LLS-RXN	8.33 m	19.40 (0.00)	19.40 (0.00)	19.40 (0.00)
	12.5 m	19.38 (0.00)	19.38 (0.00)	19.38 (0.00)
	25.0 m	19.31 (0.00)	19.31 (0.00)	19.31 (0.00)

668

669

670

671

672

673

674

675 Table A2

676 Absolute BIAS values ($\text{Mg}\cdot\text{ha}^{-1}$) for the different models and resolutions. Fitting resolution is by rows
 677 and prediction resolution by columns. Negative values denote an underestimation and positive values an
 678 overestimation (eq. 18).

Model		Plot size	Predict		
			8.33 m	12.5 m	25.0 m
LLS-XR	Fit	8.33 m	-0.03	0.13	0.23
		12.5 m	-0.18	-0.02	0.07
		25.0 m	-0.23	-0.09	-0.01
LLS-XNR	Fit	8.33 m	-0.04	1.59	3.31
		12.5 m	-1.48	0.00	1.59
		25.0 m	-2.84	-1.47	0.02
NLS-XR	Fit	8.33 m	-0.02	-0.77	-1.61
		12.5 m	0.61	0.06	-0.60
		25.0 m	1.06	0.60	0.05
NLS-XNR	Fit	8.33 m	-0.03	1.63	2.85
		12.5 m	-1.44	0.06	1.18
		25.0 m	-2.47	-1.03	0.08
LLS-RXN	Fit	8.33 m	-0.14	-0.14	-0.14
		12.5 m	-0.12	-0.12	-0.12
		25.0 m	-0.13	-0.13	-0.13

679